

Modeling of corona-induced electrohydrodynamic flow with COMSOL multiphysics

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Abstract —Electrohydrodynamic (EHD) flow is a flow of electrically neutral gas caused by corona-generated ions drifting through it. Many aspects of this gas movement phenomenon such as electric field and charge distribution, fluid dynamics, and heat transfer have been investigated, and the use of accurate models have become critical in the development of commercial applications in this field. The purpose of the present paper is to demonstrate that corona induced airflow can be successfully modeled using COMSOL multiphysics, a commercial software package that performs equation-based multiphysics modeling for different physical processes by applying the finite element method to the system of partial differential equations. Governing equations, boundary conditions, and numerical results obtained with COMSOL multiphysics are presented, and compared with experimental results. Numerical results are found to be in good agreement with experimental results.

I. INTRODUCTION

Electrohydrodynamic (EHD) flow is a flow of electrically neutral gas caused by corona-generated ions drifting through it. Many aspects of this gas movement phenomenon such as electric field and charge distribution, fluid dynamics, and heat transfer were extensively studied over a wide range of potential electrostatic fluid accelerator (EFA) applications, including electronics cooling, air filtration, air movement, and many others [1-9]. However, EHD flow involves interaction between electric field, ion motion, flow of electrically neutral gas molecules, and is described by a system of coupled nonlinear equations. Since analytical solutions can be obtained only for a very limited number of cases with the simplest geometry, numerical modeling of EHD flow has become essential for the development and optimization of technologies in the EHD field. Although several

numerical techniques and approaches have been developed, many of them have limitations, use some simplifications, require prior experimental data, or are simply not convenient to use. As the EFA field continues to evolve, there is a growing need for accurate models that can help predict device performance metrics, such as corona onset voltage, current-voltage curves, power consumption, air velocity profiles, back pressure, and heat exchange. Many previous modeling efforts only account for electrostatic interactions [10]. For accurate modeling, however, it is important to include effects of fluid dynamics and the complete space charge transport equation. Preliminary coupled-physics modeling has been conducted in one-dimensional space without accounting for charge generation showing good agreement with analytical models for a simple one-dimensional space [11]. The modeling problem becomes especially challenging for design and optimization of EFA devices with high geometric complexity. Several investigations into corona based EHD flow and convective heat transfer modeling have been presented recently, however most lack a rigorous comparison with experimental current-voltage, airflow, and air velocity profile results [4,12].

The purpose of the present paper is to demonstrate that corona based ion current and induced airflow can be successfully modeled for a complex geometry using COMSOL multiphysics, a commercial software package that performs equation-based multiphysics modeling for different physical processes by applying the finite element method. Numerical results are presented and compared to experimental results from a representative EHD device in order to validate the model. A brief background into corona-induced air flow is presented, followed by a description of the numerical and experimental models, and finally concluded with a comparison and discussion of numerical and experimental results.

II. BACKGROUND

The mechanism of corona-induced ionic wind propulsion is illustrated in Fig. 1. Gas molecules near the corona discharge region become ionized when a high intensity electric field is applied between a high tip curvature corona electrode and a low tip curvature collector electrode. In the case of a wire or rod electrode, the radius of curvature of the cross-section along the diameter of the wire or rod electrode is equivalent to the tip curvature of a needle electrode. The ionized gas molecules travel towards the collector electrode, colliding with neutral air molecules. During these collisions, momentum is imparted from the ionized gas to the neutral air molecules, resulting in the movement of gas towards the collector electrode.

The operating voltage range for corona discharge lies between the corona onset and the air gap breakdown voltage [13]. Corona induced airflow is possible with both positive and negative voltages and polarities. In general, the selection of polarity depends on a large number of factors, which include electrode material, device geometry, ozone generation constraints, and others. The governing equations describing the interaction of electric charges with moving media in an electrostatic fluid accelerator have been known for a long time and comprehensive reviews and tutorials on this subject are readily available [13-19].

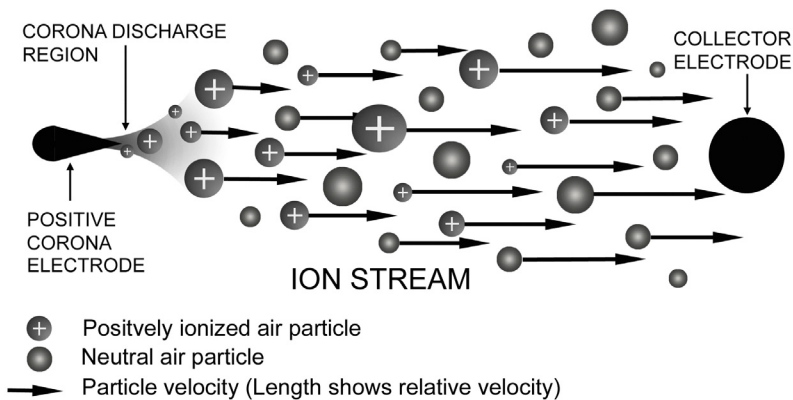


Fig. 1. Ion stream of a DC electrostatic air pump, where a high voltage is applied between the corona and collector electrodes.

III. NUMERICAL MODELING

A. Governing equations for electrohydrodynamic flow

Electrohydrodynamic flow induced by corona discharge and is described by the following equations. The electric potential V is governed by Poisson's equation

$$\nabla^2 V = -\frac{\rho}{\epsilon_0} \quad (1)$$

where ρ is the space charge density and ϵ_0 is the dielectric permittivity of free space. The electric potential is defined from electric field intensity \mathbf{E} as

$$\mathbf{E} = -\nabla V \quad (2)$$

Electric current in the drifting zone is a combination of three effects: conduction (motion of ions under electric field relative to entire airflow), convection (transport of charges with airflow), and diffusion. Therefore, current density \mathbf{J} is given by

$$\mathbf{J} = \mu_E \mathbf{E} \rho + \mathbf{U} \rho - D \nabla \rho \quad (3)$$

where μ_E is the air ions mobility in an electric field, \mathbf{U} is velocity vector of airflow, and D is the diffusivity coefficient of ions. Current continuity condition gives equation for current density

$$\nabla \cdot \mathbf{J} = 0 \quad (4)$$

The fluid dynamic part of the problem is described by the Navier-Stokes equations and continuity equation for steady state incompressible air flow

$$\rho_{air} \mathbf{U} \cdot \nabla \mathbf{U} = -\nabla p + \mu \nabla^2 \mathbf{U} - \rho \nabla V \quad (5)$$

$$\nabla \cdot \mathbf{U} = 0 \quad (6)$$

where ρ_{air} is the air density, p is the air pressure, and μ is the air dynamic viscosity. The system of equations (1), (3), (4), (5), and (6) is subject to appropriate boundary conditions described below for EHD device investigated in this study.

B. Space charge generation

Space charge generation by corona discharge in an EFA device can be modeled by applying appropriate electrostatic and charge transport boundary conditions at the surface of the corona electrode and ionization zone. A description of the boundary conditions for space charge generation estimation is described in this section.

The gap between corona and collecting electrodes can be divided into two regions, the ionization and drift zones. The ionization zone exists in close proximity to the corona electrode, in which air ionization occurs, and both positive and negative ions exist. The drift region, located outside the ionization zone, contains ions of a single polarity that have been driven out of the ionization region by the electric field. When the radius of the corona electrode is much smaller than the distance between corona and collecting electrodes, the ionization zone forms a uniform sheath over the coronating region of the corona electrode surface. For the positive corona, the electric field strength E_e at the surface of a smooth corona electrode of radius R_e is given by Peek's empirical formula for air at standard conditions [13]

$$E_e = E_0 \left(1 + 2.62 \cdot 10^{-2} / \sqrt{R_e} \right) \quad (7)$$

where the corona electrode radius R_e is measured in meters and $E_0 = 3.31 \cdot 10^6$ V/m is the breakdown (ionizing) electric strength of air. In contrast with the drifting zone, the ionization zone contains charges of both polarities. However due to the large difference in motilities between electrons and positive ions, the vast majority of the ionization region volume has a net space charge, which is positive in the case of a positive corona [20]. Thus, the model presented in this paper ignores the effect of the bipolar region of the ionization zone by assuming its bipolar region thickness is zero.

At the external surface of the ionization zone, Kaptsov's assumption is made [21], which states that the ionization zone radius and electric field strength on the wire surface remains approximately constant with a changing V_e once a corona is formed. This enables estimation of the surface charge density on the external surface of the corona wire by specifying electric potential V_e and assuming the electric field strength $E = E_e$ at the surface of the corona wire.

C. Model geometry under test

A wire-to-grid channel EFA geometry was used for this study and consists of three major components, a corona electrode, collecting mesh, and collecting side walls, as shown in Fig. 2. The corona electrode is a conductive wire with a constant radius of curvature along its length which is centered between and parallel to two conductive plates that make up the collecting side walls of the channel. A collecting mesh consisting of parallel conductive wire electrodes is placed within the channel down stream and parallel to the

corona electrode and orthogonal to the airflow path. The electrodes in the collecting mesh are spaced close together such that the electric field strength at their surface is reduced below the corona onset requirement, while at the same time creating only a low pressure drop to the airflow passing through the mesh.

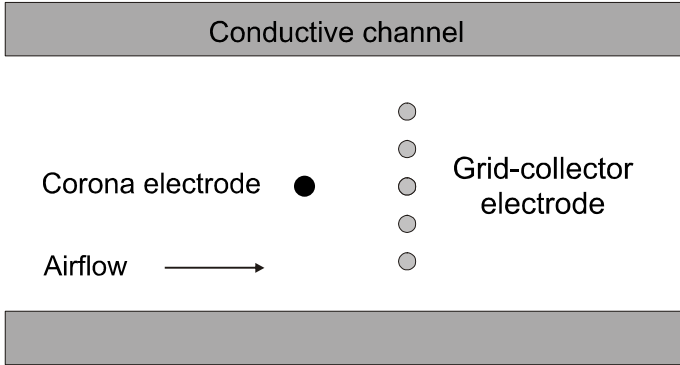


Fig. 2. Diagram of wire-to-grid channel concept; not drawn to scale.

Physical measurement of average air velocity at the output of the channel is relatively simple since the air velocity is fairly uniform across the output of the channel, which would not necessarily be the case if the grid collector electrodes were replaced with a single or multiple rod of larger diameter. A channel geometry was chosen such that it enables simple measurement of the total volume of airflow produced from the EFA device, which would be difficult in the case of an open system without a channel to confine the flow. The conductive channel geometry allows for maximum collection of ions produced by the corona discharge by creating a large surface over which collection can occur, thus increasing the accuracy of corona current measurements during operation.

By utilizing a conductive channel, the boundary conditions at the surface of the channel are simplified. Had a dielectric surface been used for the channel, there would be ion adhesion to the channel wall creating a surface charge that would have to be accounted for in the numerical model. Although such modeling is possible, it adds additional complexity and sources of error, which should be minimized for model validation purposes.

D. Numerical solution domain and boundary conditions

The wire-to-grid channel EFA numerical simulation space, subdomains, boundaries, and mesh are shown in Fig. 3. A single subdomain was used for the entire simulation space which made up the inside of the channel, where the electrical, charge transport, and fluid dynamic domain equations were solved using the subdomain modeling parameter values shown in Table 1.

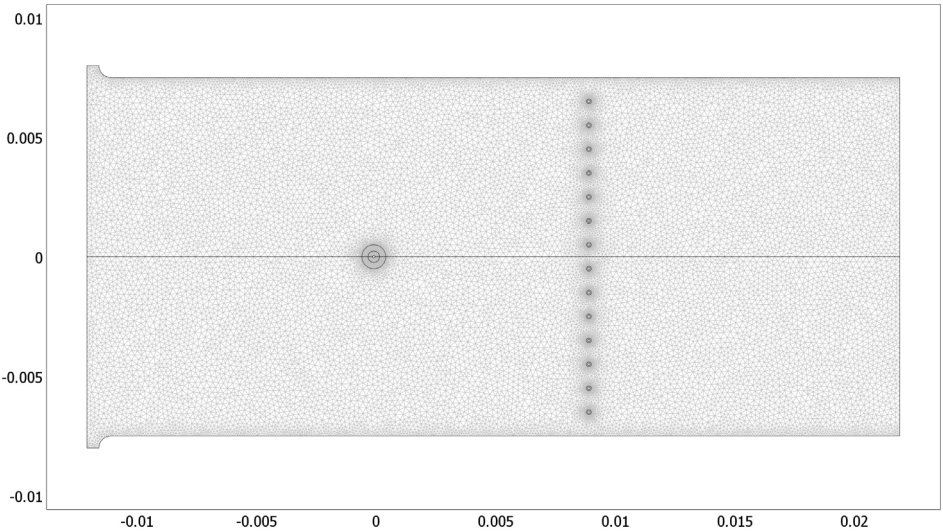


Fig. 3. Numerical solution domain and mesh of wire-to-grid channel EFA geometry. The corona electrode is represented by the smallest of the three concentric circles centered at (0,0). The two larger concentric circles were used to define mesh refinement but do not represent actual boundaries.

Table 1. Sub-domain modeling parameter values used in FEM modeling

Modeling parameter	Value
Relative dielectric permittivity of air, ϵ_r	1
Charge diffusion coefficient, D	$5.3 \times 10^{-5} \text{ m}^2/\text{s}$
Ion mobility coefficient, μ_E	$1.8 \times 10^{-4} \text{ m}^2/(\text{Vs})$
Density of air, ρ_{air}	1.23 kg/m^3
Dynamic viscosity of air, μ	$1.8 \times 10^{-5} \text{ Ns/m}^2$
Corona electrode to channel electrode separation	7.5 mm
Corona electrode to grid collector minimum separation	9 mm
Corona electrode radius	50 μm
Collecting grid wire electrode radius	50 μm

Boundary conditions applied to the numerical model are as follows. For electrostatics, a constant positive DC voltage V_e was applied to the corona wire surface, and zero volts were applied to the channel wall and surface of all collecting grid wires. For charge transport, a space charge surface density is applied to the surface of the corona wire. A zero diffusive flux condition is imposed on all boundaries except for the surface of the corona wire. The validity of this assumption is justified by the fact that the diffusion term is very small compared to the conduction term in (3) and can be set to zero at the boundaries with negligible effect [22,23]. For fluid dynamics, a no-slip condition is applied to

the surface of the channel, collecting grid wires, and corona electrode. Normal flow with pressure prescribed from Bernoulli's equation was used at the channel input air boundary, and an outlet-flow condition and zero pressure was prescribed at the outlet air boundary. The numerical simulation space was discretized in approximately 44,000 triangular elements, with the element density being highest in the region around the corona electrode and in the areas of relative high space charge density and electric field intensity, as shown in Fig. 3.

IV. EXPERIMENTAL MODEL DESIGN AND TEST PROCEDURE

A. *Experimental model design*

The wire-to-grid channel EFA geometry shown in Fig. 2 and Fig. 3 was used as a basis to construct the experimental model shown in Fig. 4. The top and bottom collecting plates were constructed of flat rectangular aluminum bar stock with a cross-section width and length of five millimeters and thirty four millimeters respectively, and an overall length of thirty centimeters. The corona and collecting electrode wires were held in place ten millimeters from the outlet plane of the device by wire spacing structures attached to either end of the top and bottom collecting plates. The wire spacing structure was made from a custom PCB board ensuring accurate mutual and absolute placement of the corona and collecting wire electrodes relative to themselves and the collecting plates. Fourteen tungsten 100 micrometer diameter collecting wires were strung one millimeter apart on center from the top to the bottom of the channel made by the collecting plates, creating a total channel gap of fifteen millimeters. A single tungsten corona wire electrode of same diameter was placed parallel to the collecting wires and centered between the collecting plates, with a distance from the collecting wires of nine millimeters, and a total coronating wire length of 27.7 centimeters. To ensure proper tensioning of the corona wire during operation, a spring based wire tensioning system was used at one end of the channel.

B. *Experimental test setup and procedure*

Current-voltage and output air velocity profile measurements were taken from the wire-to-grid channel EFA prototype using the experimental test setup shown in Fig. 4. In operation, the corona electrode of the prototype was connected to the output of a positive polarity high voltage power supply, and the collecting plates and wires were connected to ground. Voltage and current measurements on the corona electrode were measured using the built in current and voltage measurement capabilities of the Spellman SL high voltage power supply. All measurements were conducted in ambient air at room temperature and pressure.

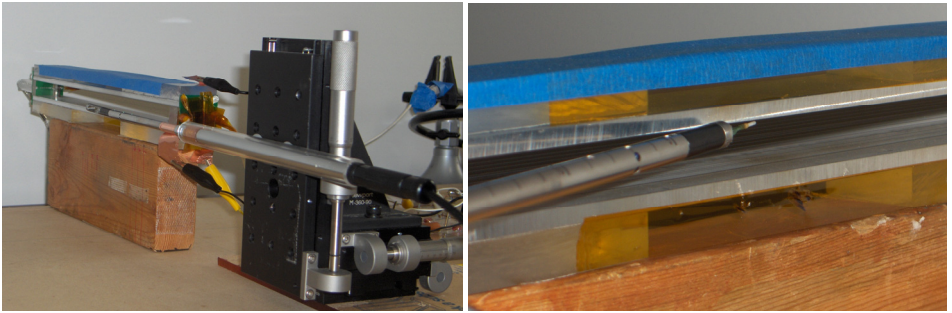


Fig. 4. Left shows picture of the experimental test setup for the wire-to-grid channel prototype current-voltage and airflow profile measurements. Prototype wire-to-grid channel EFA device and stand, hot wire anemometer, and XYZ precision stage are shown, with high voltage DC power supply with and DAQ PC out of picture. Right shows close-up view of the channel output with hot wire anemometer.

Airflow measurements were taken at the midpoint along the length of the prototype such that any fluid dynamic edge effects from the side walls at either end would not impact the air velocity profile or magnitude at the point of measurement. At the midpoint of the device the airflow measurements were taken immediately inside the output of the device, and were taken from one millimeter from the top of the channel to one millimeter from the bottom of the channel at one half millimeter increments. Measurements were taken no closer than one millimeter from the collecting plates due to size restriction of the anemometer probe. For each measurement point ten data samples were collected and averaged. Air velocity measurements were taken with a TSI Velocicalc Plus hotwire anemometer.

V. NUMERICAL AND EXPERIMENTAL RESULTS

Numerical simulations results for the wire-to-grid channel geometry are presented for device electric field profile, charge distribution, onset voltage, current-voltage curve, air velocities, and output air velocity profile. Surface plots of the investigated model shown in Fig. 5 display the solutions to the three coupled physical phenomena modeled: electrostatics, charge transport, and fluid dynamics. The plots shown in Fig. 5 were generated with a corona to collector electrode electric potential difference of 8 kV.

The electric potential map, Fig. 5 (top), has the highest electric potential at the surface of the corona electrode with electric potential decreasing in magnitude from the edge of the corona electrode to the channel walls and collecting grid. The space charge, Fig. 5 (center), is distributed with highest density near the corona electrode and decreasing in all directions, with the charge density greater in the direction of the collecting wires than in the direction of the channel input. Charge flux stream lines are shown in white in Fig. 5, showing greater charge flux in the direction of the collecting grid than towards the input. The traveling ion stream entrains airflow in the direction of the wire grid as shown in Fig. 5 (bottom), with the greatest air velocities in the region of greatest space charge density and field intensity around the corona electrode.

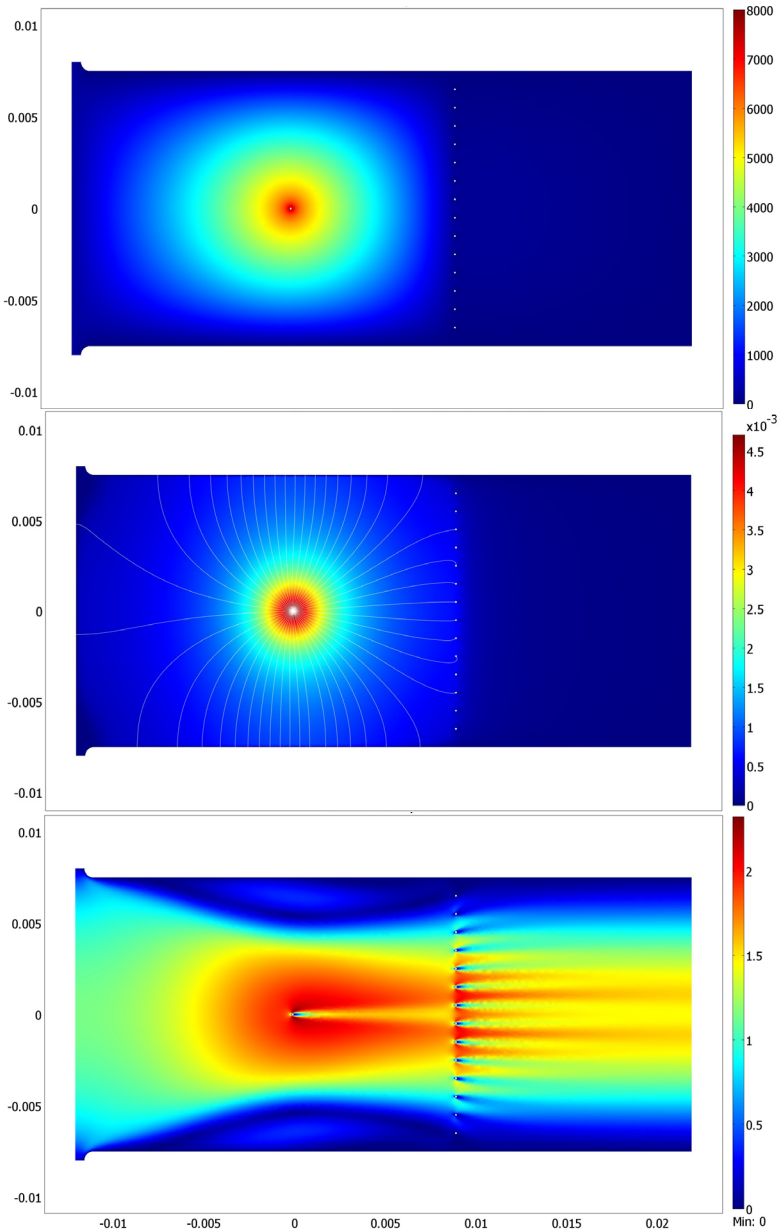


Fig. 5. Numerical simulation results: (top) electric potential as surface map with units in volts, (center) space charge density as surface map with units in C/m³, (bottom) air velocity as surface map with units in m/s. Simulation space dimensions in meters.

The corona ion current, I_c , leaving the ionization zone can be calculated by multiplying (3) by the area of the wire surface with the electric field at the surface of the corona elec-

trode, E_e . It was assumed for the calculation that the wire length was the same as the coronating wire length in the experimental model. The expected quadratic current dependence on the applied electric potential for similar geometry [10] was confirmed, and agreed well with experimentally measured corona current as shown in Fig. 6 with a maximum deviation of 4 percent occurring at a corona voltage V_c of 8 kV. The corona onset voltage V_0 also agreed well between numerical and experimental results, with onset values being 4.05 kV and 4.06 kV respectively.

Experimental and numerical average airflow velocity measurements across the output of the channel for five operating voltages from corona onset to 8 kV are shown in Fig. 7. Because experimental airflow measurements were not possible within one millimeter of the collecting plates, average airflow velocities presented in Fig. 7 are averaged from one millimeter from the bottom plate to one millimeter from the top plate. Good agreement is shown between numerical and experimental values, with the maximum deviation being 7 percent at 5 kV and the average deviation being approximately 4 percent for all points. Although good agreement is seen between average airflow velocities, some variation is seen between the experimental and numerical air velocity profiles as shown in Fig. 8. The difference between the two are likely due to slight non-symmetries in the experimental model that are not represented in the numerical model, causing the airflow profile peak to shift one millimeters toward the top of the channel and distort the shape.

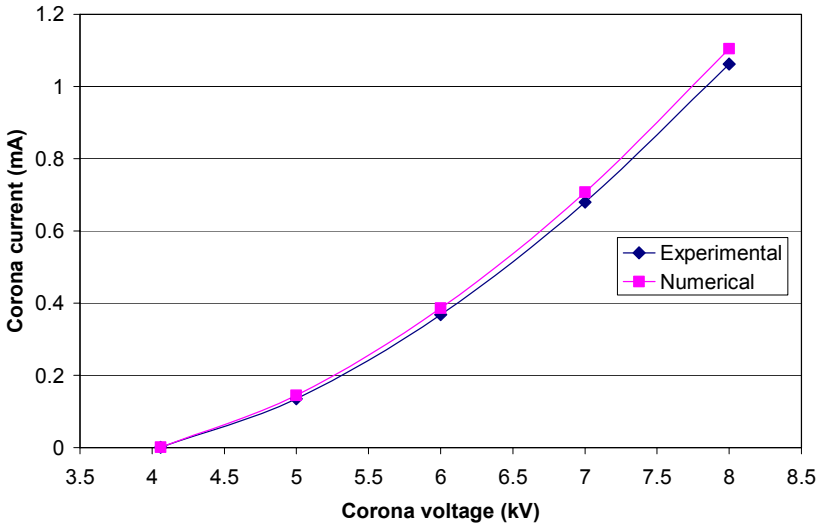


Fig. 6. Comparison of numerical and experimental corona current I_c vs. applied voltage V_c .

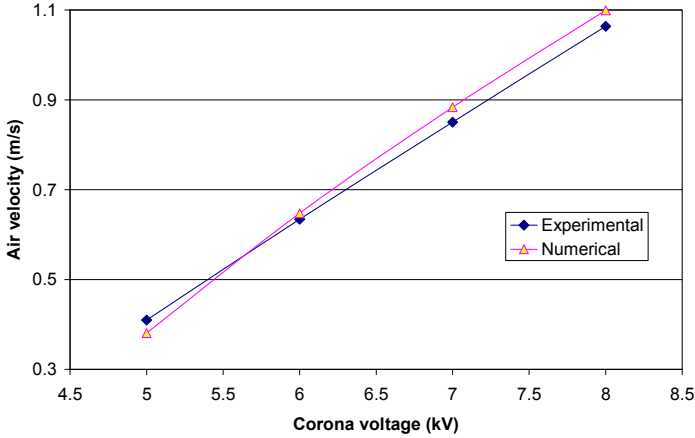


Fig. 7. Comparison of numerical and experimental average output air velocity.

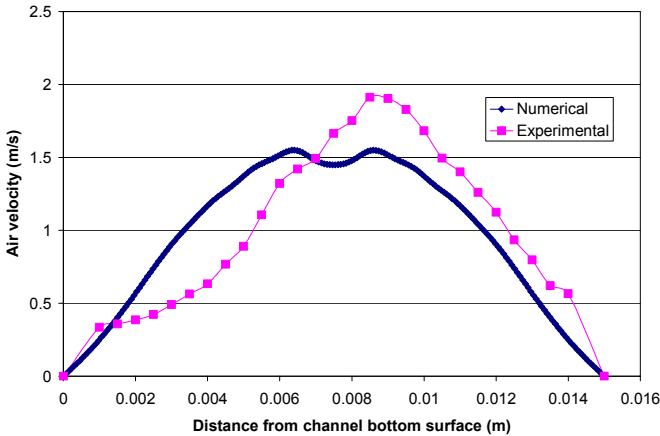


Fig. 8. Comparison of numerical and experimental output air velocity profile for an applied voltage V_e of 8 kV.

VI. CONCLUSION

A numerical couple physics model for corona-induced electrohydrodynamic flow modeled in COMSOL multiphysics was presented. Numerical model results were compared with experimental results for the same configuration and agreed well with each other, including corona onset voltage, corona ion current-voltage curve, average output airflow, and output airflow profile. Future work will focus on validation of the model over other geometries, include effects of ion attachment and charging on dielectric surfaces, and prediction of EFA driven heat transfer.

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